

MadPattern 1.0 Cheat Sheet

How Transformations of A Cell Create Patterns (...and THANK GOD we don't have to do it manually!)

Using MadPattern Templates:

The Cell
Draw in this area to be transformed into patterns.

The Tile
Export the rectangular unit as a tiling image.

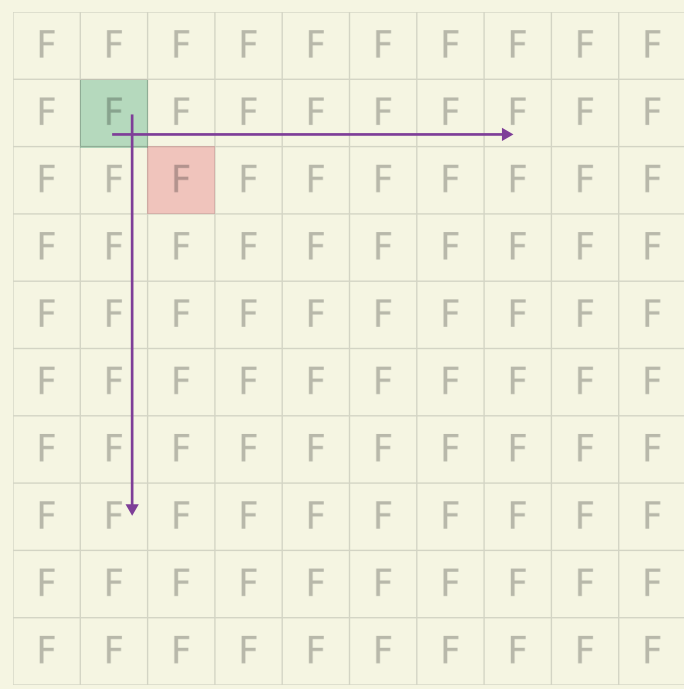
Magic Behind MadPattern:

Sets of Translations
1 → Translation Direction

Sets of Reflections
↔ Reflection Axis

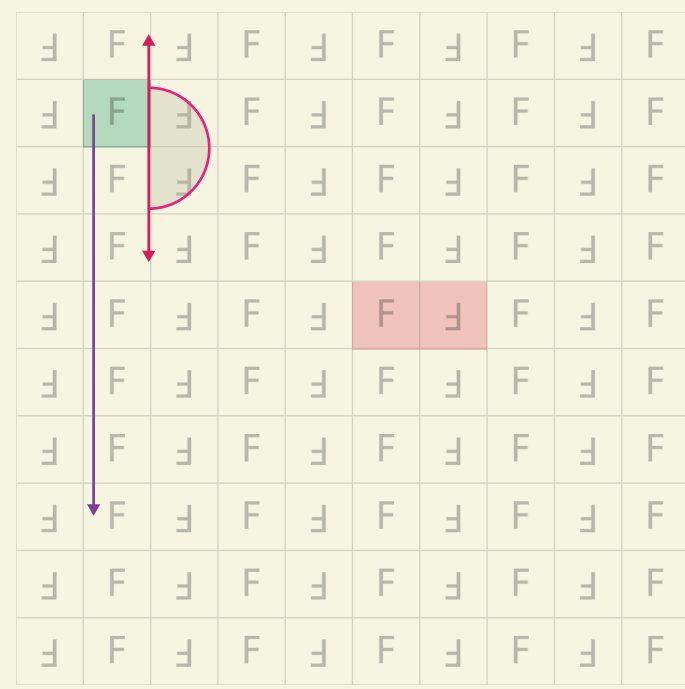
Sets of Glide-Reflections
↔ Glide-Reflection Axis

Sets of Rotations
60° 120°
90° 180°



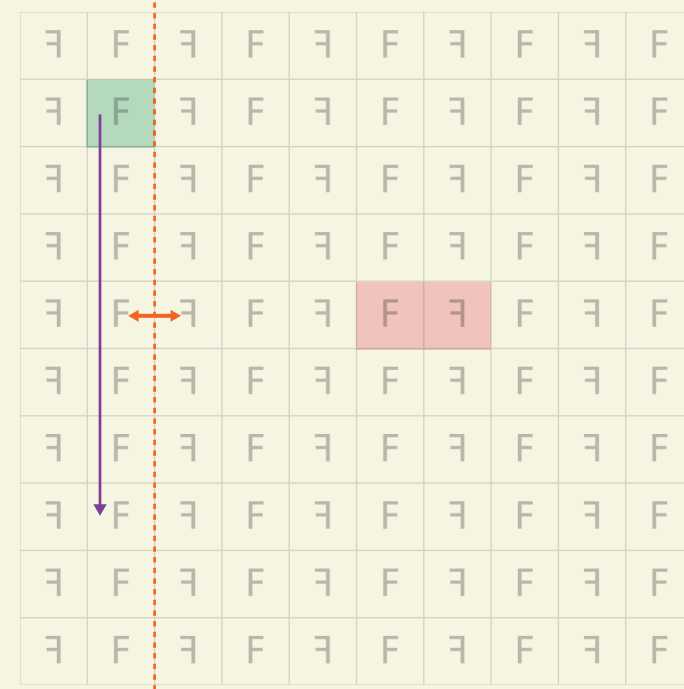
p1 → → ↔ ↻

This is the most basic form of repetitive tiling, consisting only of translations. No reflections, glide-reflections, nor rotations. The two translation axes may be inclined at any angle to each other.



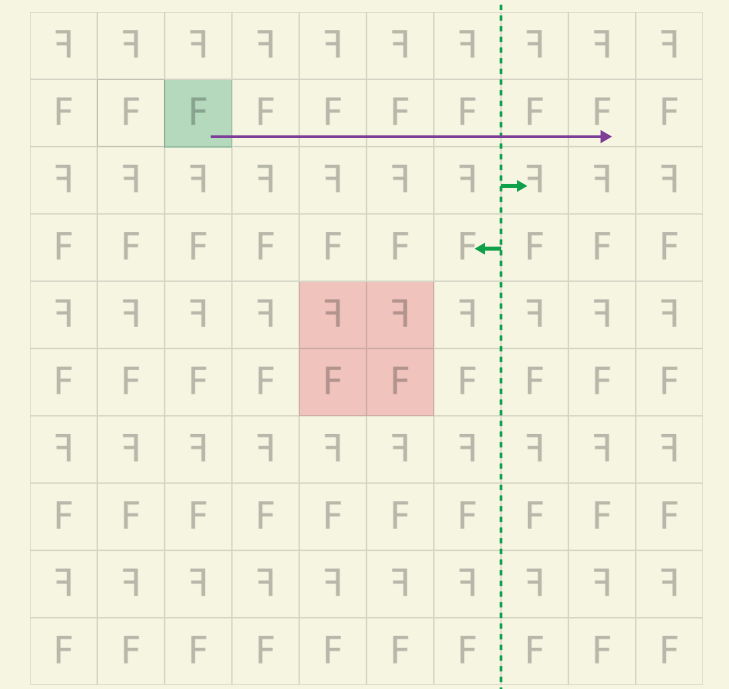
p2 → ↔ ↻ ↻

Tiling of this type, in addition to having a repeating cell, can also be turned upside down and remain the same.



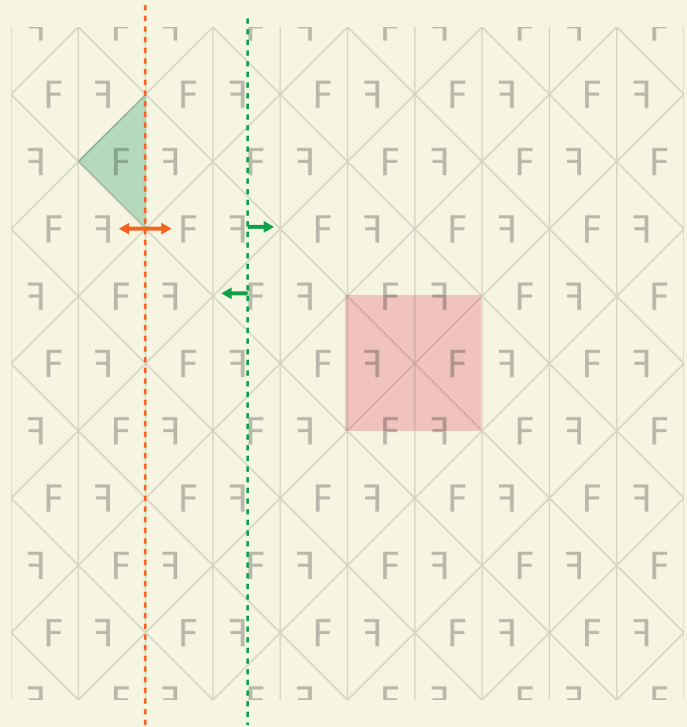
pm → ↔ ↻ ↻

This kind of tiling can be mirror-reflected along one axis. The lattice must be rectangular or square.



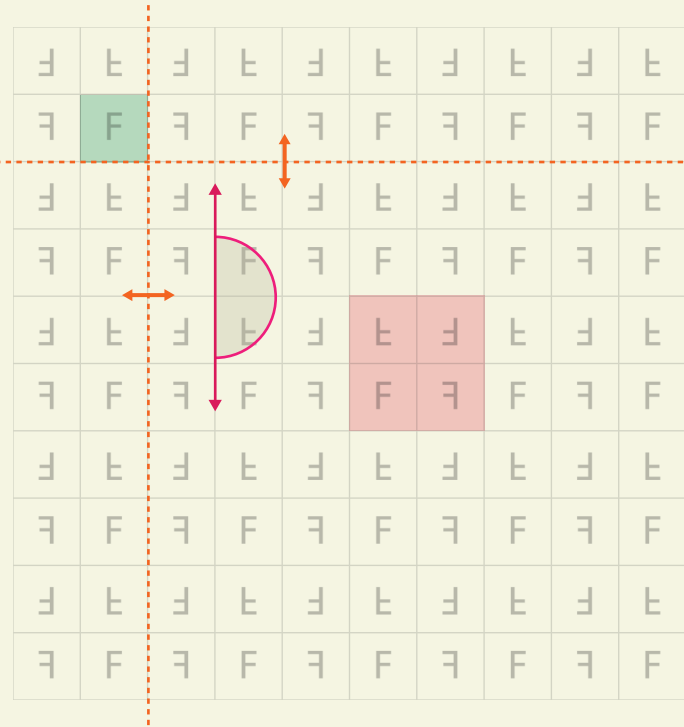
pg → ↔ ↻ ↻

This kind of tiling has a glide reflection; The tiling can be completely unchanged if it is both reflected and translated at the same time. The lattice must be rectangular or square.



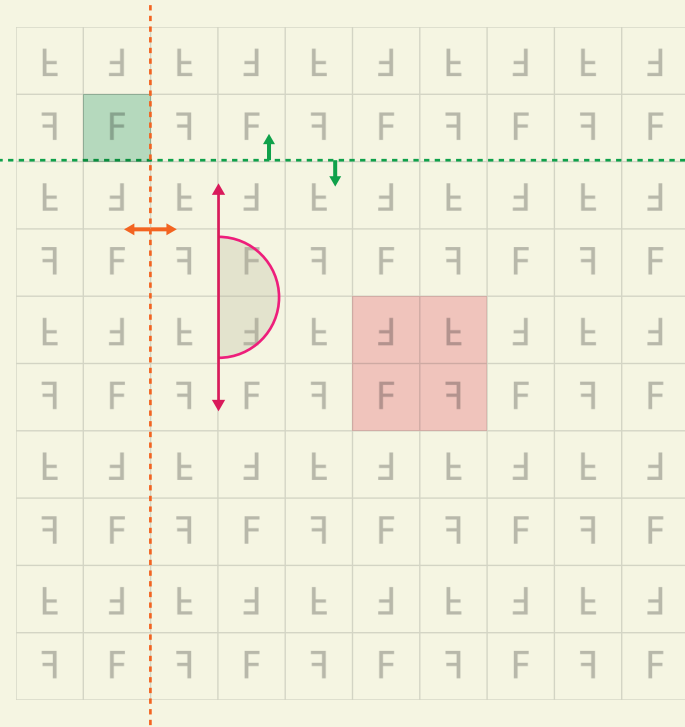
cm → ↔ ↻ ↻

This tiling has both reflections and glide reflections, the axes of which are parallel. The lattice must be a rhombus.



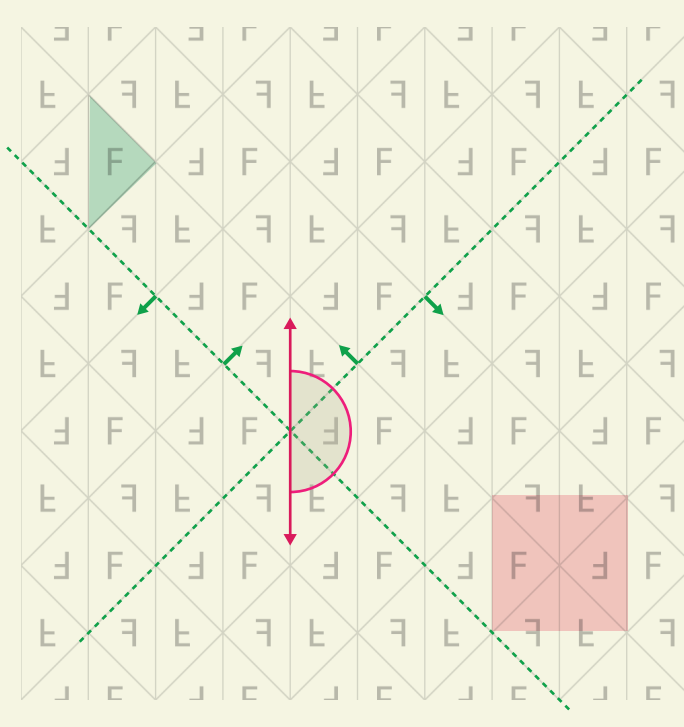
pmm → ↔ ↔ ↻ ↻

There are two sets reflection axes. As a result it can turn upside down and remain the same, and the lattice must be rectangular or square in shape.



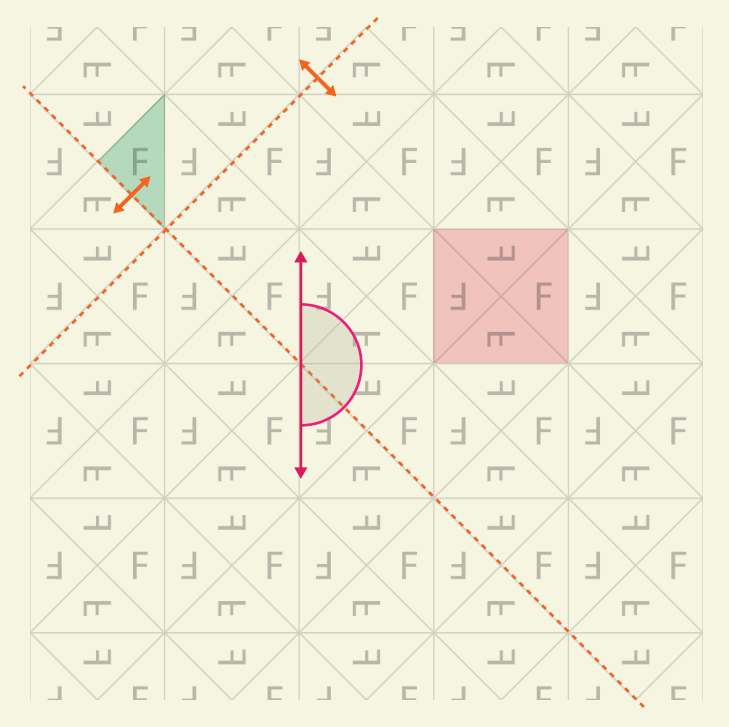
pmg → ↔ ↔ ↻ ↻

There is 1 set of axes of reflection, and can be turned by 180°. As a result, it also has a glide reflection, and the lattice must be square or rectangular.



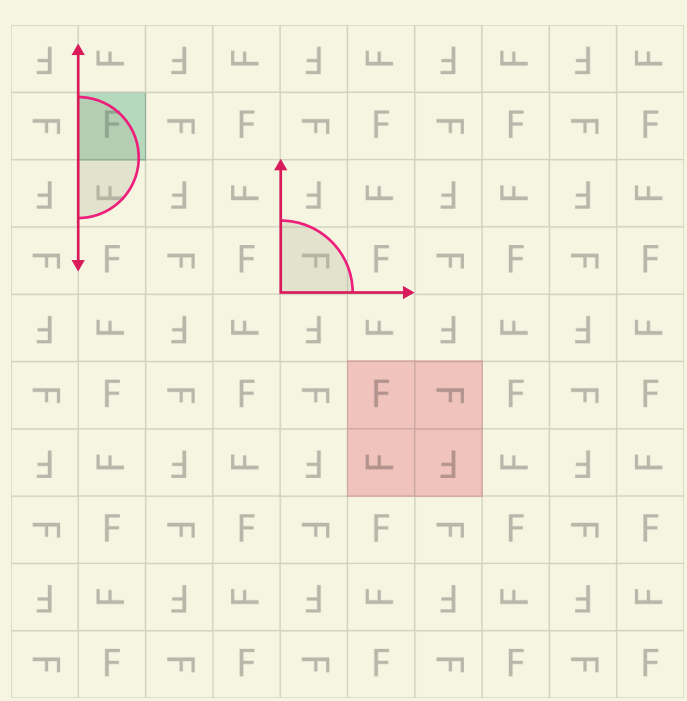
pgg → ↔ ↔ ↻ ↻

This type of tiling has glide reflections in two directions, and can also turn 180°. The lattice must be rectangular or square.



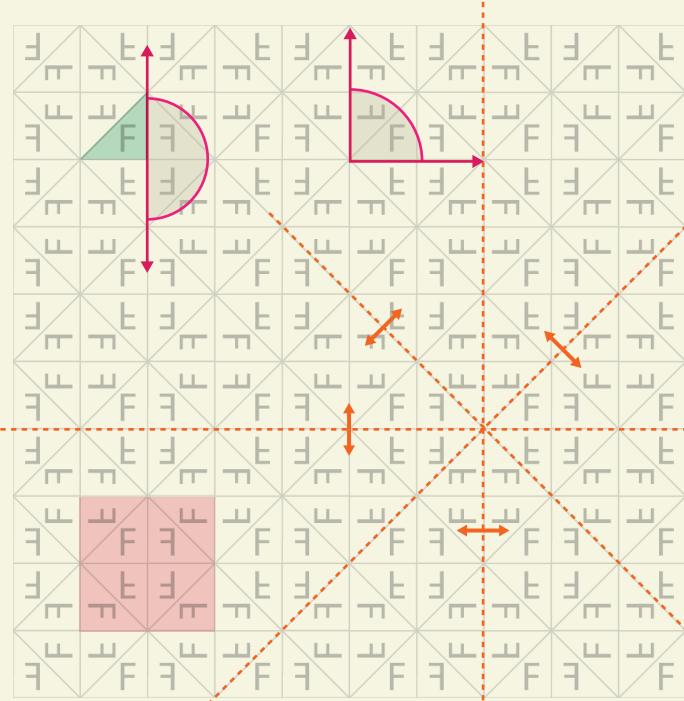
cmm → ↔ ↔ ↻ ↻

There are two sets of reflection axes. As a result this tile can turn upside down. Some pivot points may not lie on an axis of reflection. The lattice must be a rhombus.



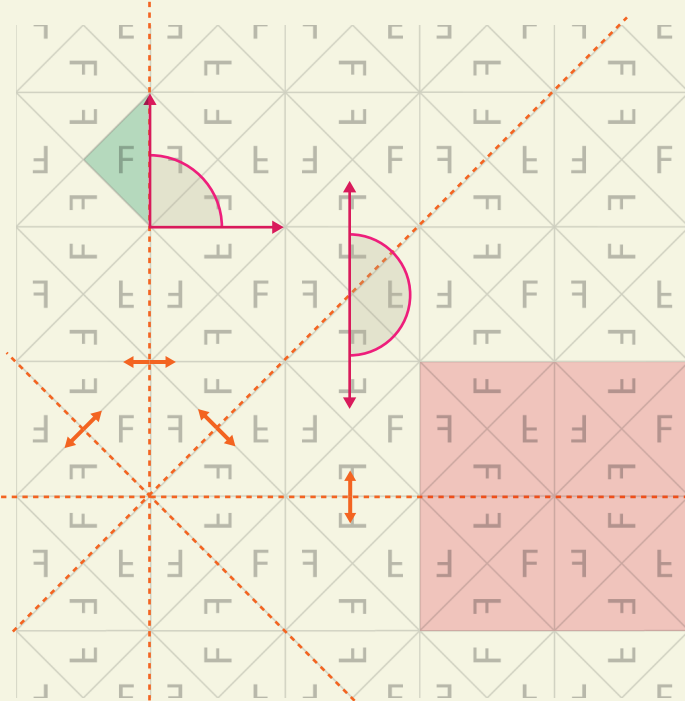
p4 → ↔ ↔ ↻ ↻

This tiling can rotate 180° and remain the same. The lattice is a square. There are also pivot points which only allow 90° turns.



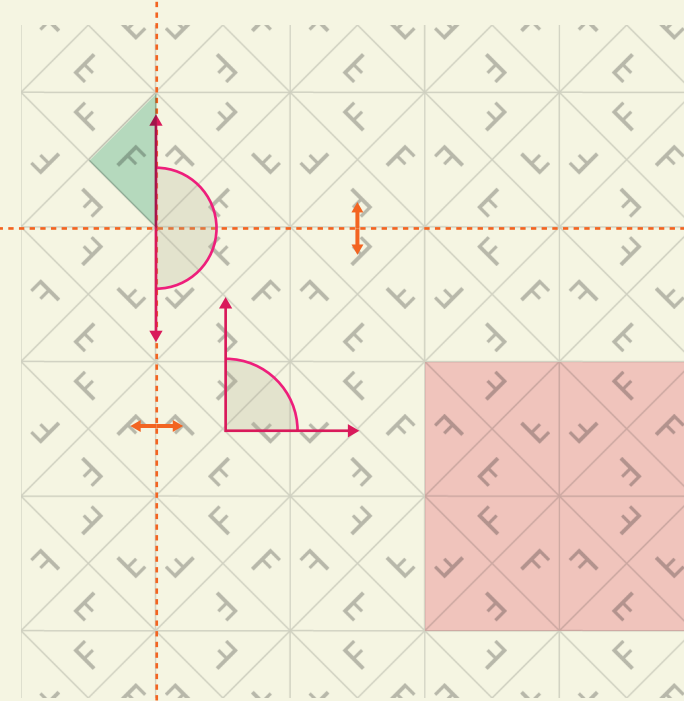
p4m → ↔ ↔ ↔ ↻ ↻

(p4m) inherits attributes from (p4), and has 4 sets of reflection axes. The pivot points of every possible rotation lie on at least one of the reflection axes.



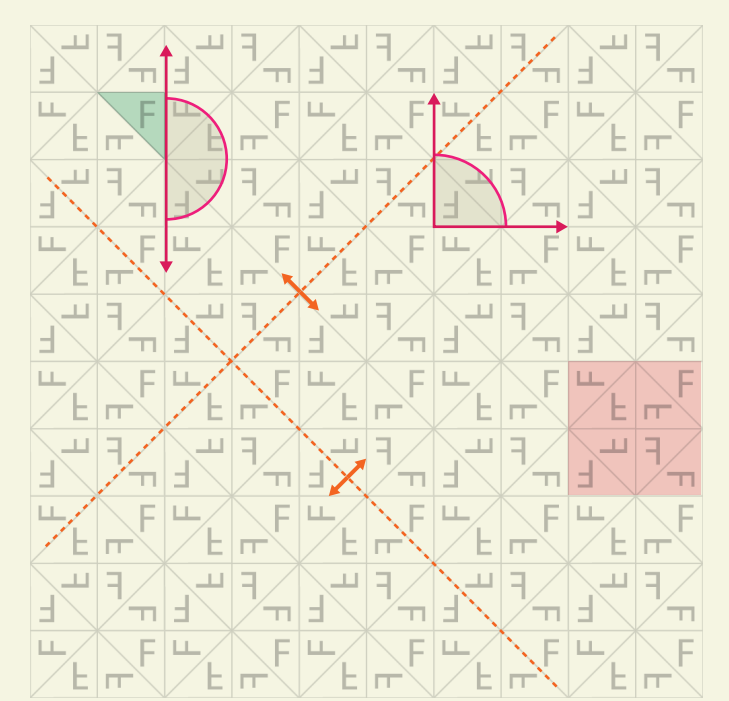
p4m rotated → ↔ ↔ ↔ ↻ ↻

A rotated version of (p4m) created a tile that invites more dynamics of symmetries.



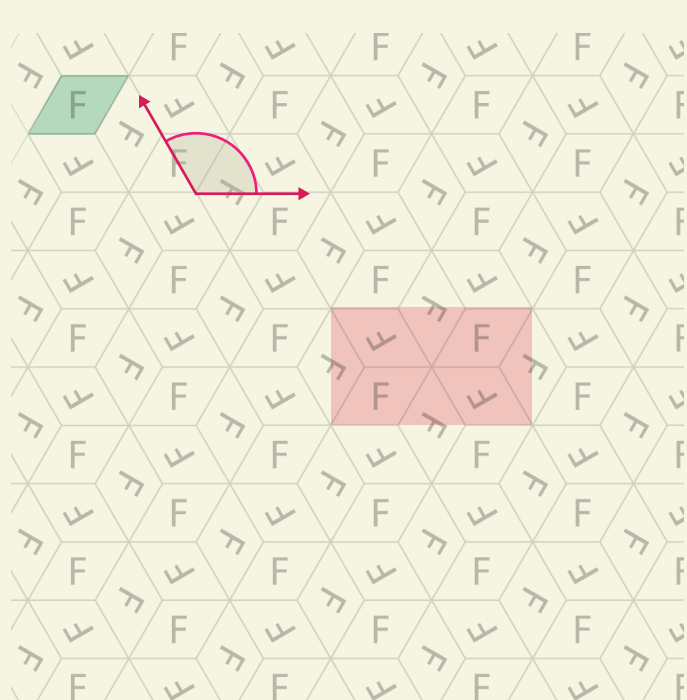
p4g → ↔ ↔ ↔ ↻ ↻

(p4g) has 2 sets reflection axes. The pivot points for 90° rotation do not lie on the reflection axes, but there are pivot points for 180° rotations only, which do lie on the axes of reflection.



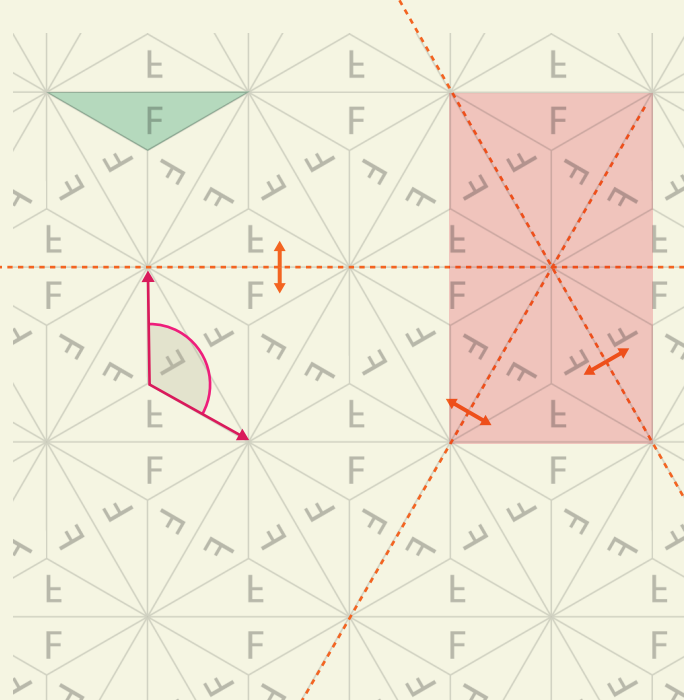
p4g rotated → ↔ ↔ ↔ ↻ ↻

A rotated version of (p4g).



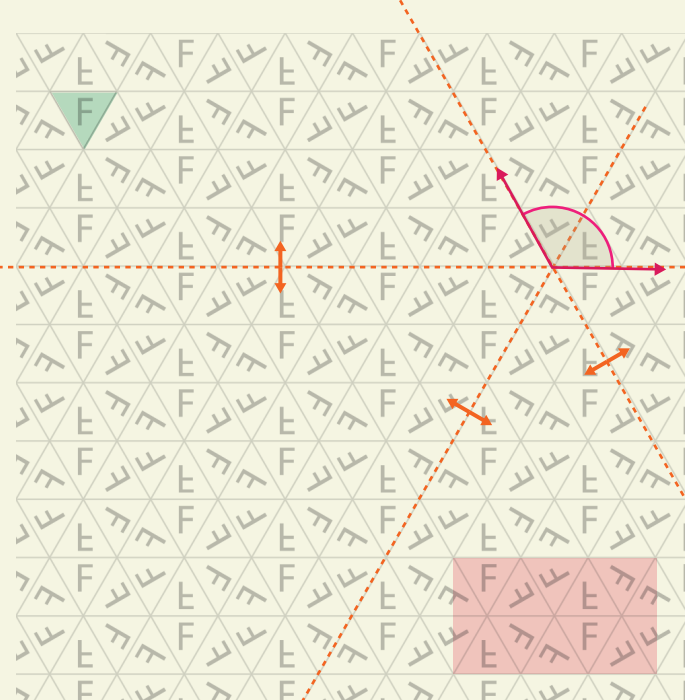
p3 → ↔ ↔ ↔ ↻ ↻

(p3) is symmetrical under rotations of 120°, but have no reflections. The lattice is hexagonal. The rotation centers can be found at the corners, as well as the centers of the hexagon.



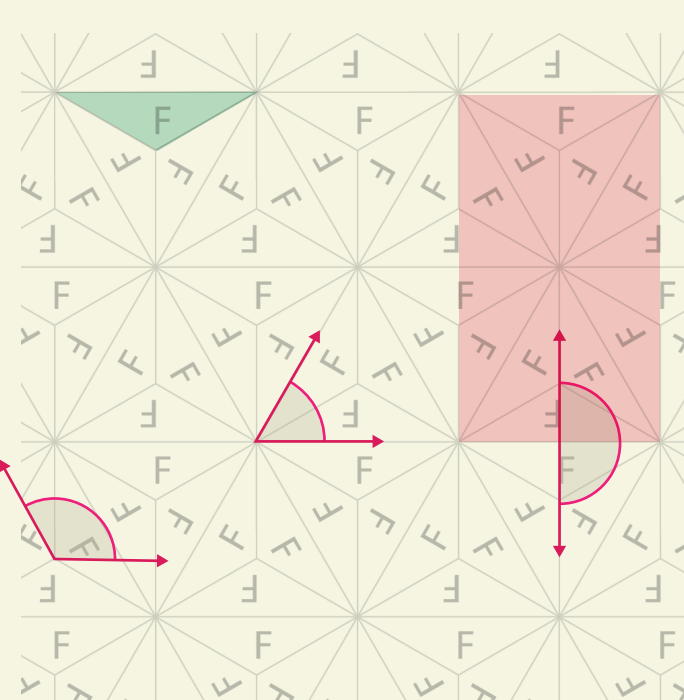
p31m → ↔ ↔ ↔ ↔ ↻ ↻

Within a hexagonal lattice, (p31m) has a 120° rotation and 3 sets of reflection axes. The distinguishing feature of (p31m) is that not all the possible rotation centers lie on a reflection axis.



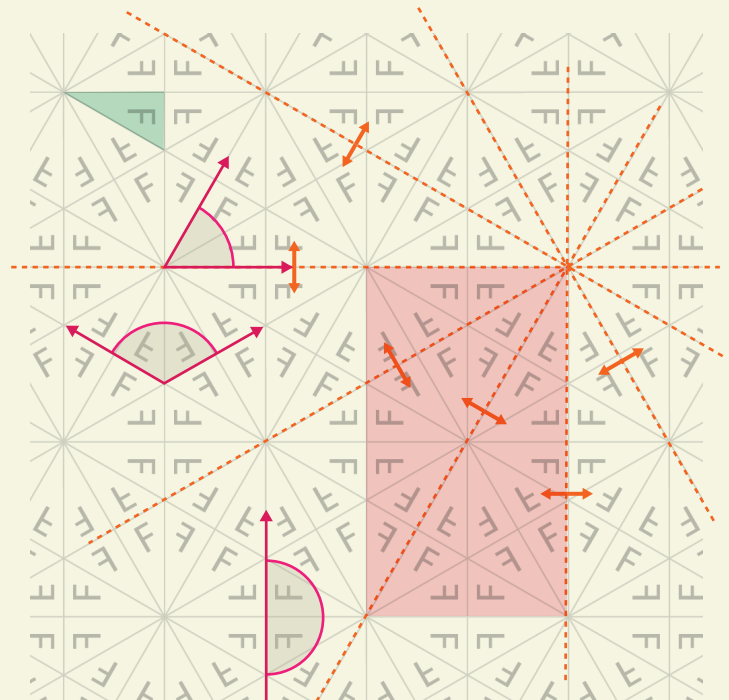
p3m1 → ↔ ↔ ↔ ↔ ↻ ↻

Sharing similar attributes as of (p31m), though all the possible rotation centers of (p3m1) lie on reflection axes.



p6 → ↔ ↔ ↔ ↔ ↔ ↔ ↻ ↻

Within a hexagonal lattice, (p6) allows 60° rotations. There are also pivot points either turn only 180° or 120°.



p6m → ↔ ↔ ↔ ↔ ↔ ↔ ↔ ↻ ↻

In addition to all the attributes inherited from (p6), (p6m) has 6 sets of reflection axes, and the 60° rotation centers lie on these axes.

RESOURCE

Download MadPattern Adobe Illustrator template:
<http://www.madpattern.com>
Read a complete explanation of 17 Wallpaper Groups and many more contents about tiling:
<http://www.quadibloc.com/math/tilint.htm> and
<http://www.clarku.edu/~djoyce/wallpaper/seventeen.html>

CREDIT

Cheat Sheet Poster (22" x 28") Designed by Shanfan Huang <http://shanfan.tumblr.com>
Patterns Included in MadPattern 1.0 Created by Matt Handler <http://www.matthandler.com>
17 Wallpaper Groups Explanation Cited from John Savard <http://www.quadibloc.com>
And David E. Joyce <http://www.clarku.edu/~djoyce/wallpaper/>



This work is licensed under a [Creative Commons Attribution-NonCommercial-ShareAlike 3.0 United States License](https://creativecommons.org/licenses/by-nc-sa/3.0/).

This work was released on 19 June 2011.